# **Computational Physics II**

#### Summer Semester 2025

### Lecture Topics (Prof. Sebastiano Bernuzzi)

### • Programming

- Unix & Linux
- Bash & Console navigation
- Programming languages
- Introduction to Python
- Floating point representation

### • Solving equations and Linear systems

- Root finding: Bisection, Newton-Raphson, Secant
- Direct methods: Gauss elimination, LU decomposition
- Iterative methods: Jacobi, Gauss-Seidel, Successive-Over-Relaxation

### • Function representation, integrals, derivatives

- Polynomial approximation of function, interpolant
- Runge phenomenon
- Integrals: Riemann sums, Trapezoidal rule, Gaussian quadratures
- Spectral methods: Orthogonal polynomial, Fourier basis
- Interpolation: Lagrangian, Splines
- Derivatives: finite differencing, spectral methods

### • Ordinary Differential Equations

- Initial Value Problems: well-posedness, stability and convergence
- Euler scheme: stable/unstable vs explicit/implicit
- Stability analaysis of ODE solvers
- Runge-Kutta methods
- Simplecting method: symplectic Euler, Störmer&Verlet
- Boundary Value Problems: shooting method, solution with methods for linear systems
- Fourier Transform
  - Discrete Fourier Transform
  - Fast Fourier Transform
  - Solution of BVPs via FFT
  - Signal analysis

### • Monte Carlo methods

- Random variables and pseudorandom numbers
- Multidimensional integration with MC
- Random walks and Metropolis algorithm

## **Tutorials (Aurora Capobianco)**

- Gymnastic with bash and Python
- Roots of complex functions and fractals
- Tridiagonal system solver: direct vs iterative methods
- Lagrangian Interpolation
- Finite differencing
- Kepler problem
- Ising 2D model